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## **Developing** assessment instruments to measure prospective teacher beliefs about mathematical problem solving using the Rasch model

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#### Abstract

Beliefs in solving mathematical problems becomes the basis for action, the basis for change and the basis for learning mathematics. This research describes the development of an instrument for measuring student teachers' beliefs in solving mathematical problems. A total of 160 students who had experience in problem solving and learning mathematics became research respondents. Research data was analysed using Rasch modelling. The results of data analysis show that the instrument developed is declared reliable and valid. A total of fifty-five items can be used to measure student teachers' beliefs in solving mathematical problems. The instruments that have been developed care used as initial assessments in implementing problem-based learning so that they can help students develop critical thinking and reasoning to face challenges in real life.

Keywords: beliefs; problem-solving; measure; Rasch.

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#### Introduction

Mathematical problems must be able to be solved within the framework of the maturation process that must be gone through and is a means of self-maturation to provide the problem one's existence both as an individual and as part of one's environment (Bal, 2015; Memnun et al., 2012; Muhtarom et al., 2020; Siswono et al., 2019). The ability to solve problems is a basic skill that a person must have. To solve mathematical problems, a person tries to direct his mind to recall and utilize mathematical procedures that are appropriate to the problem to be solved. Muhtarom et al., 2019; Siswono et al., 2019). Through mathematical problem solving, students are directed to develop their abilities, including building new mathematical knowledge, solving problems in various contexts related to mathematics, applying the necessary strategies and reflecting on the mathematical solving process (Arikan, 2016; Harisman et al., 2019; Mkomange et al., 2012).

Positive beliefs in solving mathematical problems are the basis for action, the basis for change and the basis for learning mathematics (Muhtarom et al., 2020). This is due to the benefits that can be obtained when problem solving is carried out by involving thought processes and self-regulation abilities, thereby enabling the development of a strong understanding and belief in problems accompanied by logical reasons. Beliefs is solving mathematical problems that influences mathematics achievement, for example: the level of difficulty of the problem, the formula to be used and the decision to recheck the solution (Siswono et al., 2017). Beliefs as a cognitive and affective construct, which is important for the problem-solving learning process (Bal, 2015; Ozturk & Guven, 2016).

Beliefs in mathematics has a direct influence on students' mathematical problem solving performance. Teaching and gender have no influence on the beliefs in problem solving of prospective mathematics teachers (Memnun et al., 2012). Furthermore, Mkomange et al., (2012) concluded that the majority of prospective mathematics teachers have positive beliefs about the importance of understanding mathematical problems, ways of solving problems and learning mathematics that emphasizes contemporary principles. Ozturb & Guven (2016) research concluded that beliefs influence the problem solving process. Students who believe that solving problems takes a short time, they can solve them by memorizing the rules. When faced with a more challenging task, students have the beliefs to solve the problem as quickly as possible within the allotted time. They assume that if they have the ability they will solve the problem quickly.

It is important to measure beliefs in problem solving. Beliefs in problem solving can be measured using various techniques such as questionnaires, interviews and observations (Dorimana et al., 2021; Prendergast et al., 2018; Sağlam & Dost, 2014; Siswono et al., 2016, 2019; Stage & Kloosterman, 1992). Several questions can be used to explore mathematics teachers' problem-solving beliefs (Siswono et al., 2016). Another study using a mixed prethods approach with 36 respondents showed that the majority of respondents showed a positive attitude towards the progress of problem solving in mathematics clarges (Dorimana et al., 2021). Sağlam's research was conducted on 413 respondents using the Beliefs about Mathematical Problem Solving instrument developed by Kloosterman and Stage and adapted into Turkish by

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Haciomeroglu (Sağlan & Dost, 2014). However, the studies above still carried out measurements using classical test theory. Item response theory, whose main component is Rasch modeling, has advantages compared to classical test theory (Rahim & Haryanto, 2021). One of these advantages is that the probability of the subject answering an item correctly depends on the subject's skills and the characteristics of the item (Adi et al., 2022). The Rasch model in analyzing instrument validity can be carried out from several aspects so that the resulting instrument can be more reliable (Andrich & Marais, 2019; Atikah et al., 2022; Indihadi et al., 2022; Saidi & Siew, 2019). Validity analysis using the Rasch model can be said to be better because of its consistency (Sharif et al., 2019; Suminton, 2018). Another advantage of Rasch modeling is that three reliabilities are obtained, namely person reliability, item reliability, and Cronbach's alpha (Sumintono & Widhiarso, 2015). The Rasch model is able to show instrument items that are difficult for respondents to agree on as well as comparing the respondent's abilities. Analysis of instrument items related to the respondent's abilities is very helpful in preparing instruments to cover the aspects to be measured (Kaspersen et al., 2017; Muntazhimah & Wahyani, 2022; Sharif et al., 2019; Sumintono & Widhiarso, 2014). Therefore, this research aims to examine the reliability and validity of beliefs instruments in problem solving for prospective mathematics teacher students using Rasch modeling.

#### Methods

This research is part of research developing an assessment of problem-solving beliefs of prospective mathematics teacher students. The respondents for this research were 160 students who were selected using the random sampling method. Respondents are students who have experience in solving mathematical problems and have taken courses in mathematics learning strategies.

-	•			
Descriptor	Positive Items	Negative Items		
3				
Beliefs about the time needed to solve the problem	1, 6, 11	16,21,26		
Steps in solving mathematical problems	2, 7, 12, 27	17, 22, 32, 33		
The relationship between mathematical concepts in	3, 13, 23, 28	8, 18, 31, 34		
solving mathematical problems				
Beliefs about various ways of solving mathematical	9, 14, 24	4, 19, 29		
problems				
Exercises to improve mathematical problem solving	5,25,30	10, 15, 20		
abilities				
Problem solving learning objectives	36, 51	41		
Views on mathema 27 s	40,50	35, 45, 55		
Questions asked in problem solving learning	57	37		
The role of students in problem solving learning	47, 49, 53, 59	39, 43, 46, 56		
The role of the teacher in problem solving learning	44, 52, 60, 58	38, 42, 54, 48		
The role of the teacher in problem solving learning	$2^{++, 52, 00, 50}$	50, 42, 54, 40		

#### Table 1. Questionnaire Grid for Beliefs in Problem Solving

The development research used is design research, development study type. The emphasis of this type of research is on development with iterative cycles using formative evaluation. The stage carried out consists of three phases, namely: initial investigation, prototype phase, and

assessment (Nieveen & Folmer, 2013; van den Akker et al 202012). In the initial investigation phase, initial observations and analysis of the concept of problem-solving beliefs are carried out. In the prototype phase, researchers designed a questionnaire including a grid and questionnaire instrument for mathematical problem solving beliefs. In detail, the grid for developing beliefs instruments in solving mathematical problems is presented in Table 1. Next, expert validation and trials of the problem solving beliefs questionnaire were carried out in the assessment phase.

Respondents' answers were measured using a Likert scale with five rating options by eliminating neutral answers. The research results were analyzed using Rasch modeling via Winsteps software version 3.73. The output used for data analysis is testing the reliability of the instrument using summary statistics, testing the validity of instrument items using output item unidimensionality, output item fit order, using a rating (partial-credit) scale with the criterion that if all ratings have a peak point then the instrument has validity (Huei et al., 2020; Saidi & Siew, 2019; Sumintono & Widhiarso, 2015), and testing instrument items that were difficult and easy for respondents to agree with.

#### Results

To determine the quality of the instrument for measuring student teacher beliefs in solving mathematical problems, several criteria must be met. The results of data processing using Winstep Rasch 3.73 software to see the reliability and validity of the instrument are presented as follows:

#### Instrument reliability

Figure 1 provides overall information about the quality of respondents, the quality of the instrument, and the interaction between person and item. Person measure = 0.36 shows the mean score of respondents in the instrument of prospective teacher students' beliefs in solving mathematical problems. An average value greater than the logit value of 0.00 indicates a tendency for respondents to answer more in agreement with statements in various items (Sumintono & Withiarso, 2014). It is clear that the Cronbach's alpha value = 0.70 is located in the interaction between the person and the item as a whole. The value of person reliability = 0.67 which is classified as sufficient and the value of item reliability = 0.99 which is classified as sufficient and the value of item reliability = 0.99 which is classified as special, so it can be concluded that the consistency of the answers from respondents is sufficient, but the quality of the items in the student teacher belief instrument is categorized as special. This shows that the instrument of prospective teacher students' beliefs in solving mathematical problems will provide relatively stable results if used by other researchers.

The average INFIT MNSQ and OUTFIT MNSQ for the person table are 1.01 and 1.03, respectively. The ideal value is 1.00 (the closer to 1.00 the better). For INFIT ZSTD and OUTFIT ZSTD the average values are 0.00 and 0.10, respectively. The ideal value is 0.00 (the closer to 0.00 the better). Likewise for the item table, the average values obtained for INFIT

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MNSQ and OUTFIT MNSQ are 1.03 and 1.03, respectively. The idea<sup>1</sup>/<sub>4</sub> value is 1.00 (the closer to 1.00 the better). For INFIT ZSTD and OUTFIT ZSTD the average values are 0.20 and 0.20, respectively. The ideal value is 0.00 (the closer to 0.00 the better).

	TOTAL			MODEL		INFIT	OUT	FIT
	SCORE	COUNT				Q ZSTD		
MEAN	195.4	60.0				1 .0		
S.D.	12.1	.0				8 1.5		
MAX.	241.0	60.0	1.50	.17		0 3.8		
MIN.	160.0		47			5 -3.5		
AODEL RM	4SE .16 4SE .15 F Person MB	TRUE SD						
AODEL RM S.E. OF erson RA RONBACH	4SE .15	TRUE SD EAN = .02 	.24 SE	PARATION N = 1.00	1.56 P	erson REI	LIABILIT	
AODEL RM S.E. OF erson RA RONBACH	4SE .15 F Person MI AW SCORE-TO ALPHA (KR- MARY OF 60	TRUE SD EAN = .02 	.24 SE	PARATION N = 1.00 E "TEST"	1.56 F	erson REI  ITY = .7(	LIABILIT'	Y .71
AODEL RM S.E. OF erson RA RONBACH	4SE .15 F Person ME AW SCORE-TO ALPHA (KR- 4ARY OF 60 TOTAL	TRUE SD EAN = .02 	.24 SE CORRELATIO 1 RAW SCOR Item MEASURE	PARATION N = 1.00 E "TEST" MODEL ERROR	1.56 P RELIABII	ITY = .70 INFIT Q ZSTD	OUT: MNSQ	Y .71
AODEL RM S.E. OF Pron RJ RONBACH SUMD	4SE .15 F Person ME AW SCORE-TO ALPHA (KR- 4ARY OF 60 TOTAL	TRUE SD EAN = .02 MEASURE ( -20) Person MEASURED COUNT	.24 SE CORRELATION a RAW SCOR Item MEASURE	PARATION N = 1.00 E "TEST" MODEL ERROR	1.56 F	ITY = .70	OUT: MNSQ	Y .71
MODEL RM S.E. OF STRON RACH SUMM MEAN	4SE .15 F Person MH W SCORE-TC ALPHA (KR- 4ARY OF 60 TOTAL SCORE 521.0 155.0	TRUE SD EAN = .02 MEASURE ( -20) Perso MEASURED COUNT 160.0 .0	.24 SE CORRELATION N RAW SCOR Item MEASURE .000 1.21	PARATION N = 1.00 E "TEST" MODEL ERROR .10 .03	1.56 P RELIABII MNS 1.0	erson RE1 ITY = .7( INFIT Q ZSTD 	OUT: MNSQ 1.03 .28	Y .71
MODEL RM S.E. OF STRON RACH SUMM MEAN	4SE .15 F Person Mi 	TRUE SD EAN = .02 -MEASURE ( -20) Perso MEASURED COUNT 160.0	.24 SE CORRELATION A RAW SCOR Item MEASURE .00 1.21 2.54	PARATION N = 1.00 E "TEST" MODEL ERROR .10 .03 .16	1.56 P RELIABII MNS 1.0 .2 2.4	erson REI 	OUT: MNSQ 1.03 .28 2.34	Y .71 FIT ZSTD .2 1.8 6.7

-----

UMEAN=.0000 USCALE=1.0000

Item RAW SCORE-TO-MEASURE CORRELATION = -.99

9600 DATA POINTS. LOG-LIKELIHOOD CHI-SQUARE: 16345.56 with 9378 d.f. p=.0000 Global Root-Mean-Square Residual (excluding extreme scores): .8484

**Figure 1.** Quality output of respondents and instruments

#### Instrument validity

2

Instrument validity is used to test whether the instrument developed can be used to measure prospective teacher students' beliefs abilities in solving mathematical problems. The tables used in the Winstep software are Item unidimensionality and item fit order. Undimensionality is an important measure to evaluate whether the instrument for prospective mathematics teacher students' mathematical beliefs developed by researchers is able to measure what it is supposed to measure (Andrich & Marais, 2019; Sharif et al., 2019; Sumintono & Widhiarso, 2015). Rasch model analysis uses principal component analysis of residuals, namely measuring the extent of diversity of instruments that measure what should be measured. Clearly presented in Figure 2 shows that the total value of raw variance in observations is 57.6%. Referring to the opinion of Sumintono & Widhiarso (2014) explains that the minimum unidimensionality requirement is 20%, the unidimensionality value in instrument development can be met. In addition, it is clear that the variance that cannot be explained by the beliefs instrument is 3.5% with an eigenvalue of 5.0.

TABLE 23.0 Keyakinan INFUT: 160 Person 60 Item REPORTED: 16	Dec 19 14:42 2023 60 Person 60 Item 5 CATS WINSTEPS 3.73
Table of STANDARDIZED RESIDUAL vari	iance (in Eigenvalue units)
	Empirical Modeled
Total raw variance in observations =	= 141.5 100.0% 100.0%
Raw variance explained by measures =	= 81.5 <mark>57.6%</mark> 58.1%
Raw variance explained by persons =	= 8.2 5.8% 5.9%
Raw Variance explained by items =	= 73.3 51.8% 52.2%
Raw unexplained variance (total) =	= 60.0 42.4% 100.0% 41.9%
Unexplned variance in 1st contrast =	= <mark>5.0 3.5%</mark> 8.3%
Unexplned variance in 2nd contrast =	= 3.0 2.1% 5.1%
Unexplned variance in 3rd contrast =	= 2.8 2.0% 4.7%
Unexplned variance in 4th contrast =	
Unexplned variance in 5th contrast =	= 2.3 1.6% 3.8%

#### Figure 2. Unidimensionality value

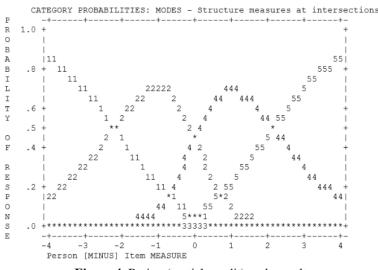
Item STATISTICS: MISFIT ORDER

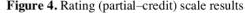
entry NUMBER	TOTAL SCORE			MODEL  IN S.E.  MNSQ					Item
10	712	160	-1.71	.14 2.40	6.712.34	6.7 A .30	.15  46.9	55.2	10
19	265	160	2.12	.1311.73	3.611.59	3.1 B.33	.17  45.6	59.31	19
48	278	160	2.12	.13 1.62	3.011.60	2.9 C .20	.191 50.0	63.11	48
5	735	160	-2.22	.1611.61	4.611.57				
29	426		63	.0711.31	3.611.29				
11	724	160	.63 -1.96	1511 26		1.9 F .17			
24	723	160	-1 04	.15 1.25	1 011 22	1 710 10	1 5 1 5 2 1	EE 41	24
18	573	160	-1.94	.08 1.17	1.011.20	2 1 17 26	.101 00.1	40.21	2.9
32		160			1.011.24	2.1 H .26	.201 30.3	42.3	10
	685				1.211.11	.7 I .39 1.3 J .22	.1/1 56.9	62.11	32
26	642	160	68		1.011.21	1.3 J .22	.21  64.4	66.81	26
3	716		-1.79			1.3 K .23			
49	702		-1.51	.14 1.16	1.011.13	.8 L .39 .9 M .33	.16  58.8	57.61	49
36	679		-1.13						
8	602	160		.08 1.11	1.0 1.15	1.2 N .15	.24  53.1	57.11	8
14	498	160	.26 1.77	.07 1.12	1.7 1.15	2.0 004	.29  6.3	9.31	14
38	287	160	1.77	.12 1.14	.8 1.10	.6 P .28	.20  60.0	64.61	38
56	402	160	51	.12 1.14 .08 1.12 .09 1.08 .07 1.05	1.3 1.12	1.3 Q .32	.29  30.6	35.71	56
28	623	160	51	.09 1.08	.6 1.11	.8 R .23	.22  64.4	64.81	28
6	492	160	.29	.0711.05	.811.11	1.6 S14	.291 6.3	9.61	6
12	449	1.60	51			1.1 T .26			
53	634	1.60	60	1011.08	611.09	6IU 13	221 66 9	66.01	53
47	440	160	56	0711 08	1 111 07	.6 U .13 .9 V .34	291 18 8	16 51	47
31	423	160	. 65	0711.06	011 00	1 01W 22	201 24 4	22 61	21
57	518	160		0711.00	211 07	017 14	201 0.4	10.01	51
				.0/11.05	- / 1 - 0 /		201 2.4	13.41	3/
2	338	160	1.21	.0911.07	. 511.05	.411 .20	.251 01.3	64.21	33
2	534	TEU	1.21 .07 OMITTED	.0/11.00	.011.07	1.0 W .22 .9 X .14 .4 Y .20 .8 Z .04	-201 10.9	19.81	2
			CONTINED	+		3 z .22		!	~~
22	501	160	- 24	.071 .97	41 .98	3 Z .22	.291 8.8	9.3	22
58	678		-1.11	.12  .96	21.96	1 y .29	.18  63.8	63.7	58
4	603		35	.081 .96		5 x .24			
33	253	160	2.35	.14  .95	3  .89	7 w .23	.16  54.4	55.81	33
1	439	160	.56	.07  .95	71 .95	6 v .15	.29  18.1	17.71	1
37	556	160				6 u .32			
43	398	160	.79	.081 .94	71 .93	7 t .44	.29  39.4	37.91	43
25	683	160	-1 19	121 91	- 51 93	3 s .21	.17  63.8	62.61	25
23	717	160	-1.81	151 92	5  .91	6 r .28	.15  60.6	54.8	23
21	384	1.60	88	081 92	- 81 .90	- 9 cr 1.8	281 50 6	46.81	21
34	423	160	. 65	.071.91	-1.11.91	-1.01p .38	.291 24.4	23.6	34
59	643	160	.88 .65 69	.101 .85	-1.01.89	710.28	211 71 3	66.81	59
	702	160	-1.51	.141 .88	71 .88	71n .26	161 61 9	57.6	9
60	688	160	-1 27	.07  .91 .10  .85 .14  .88 .13  .86 .11  .84 .11  .85	- 81 89	- 7 m 21	171 63 1	61 31	60
30	660	160	- 97	111 04	- 91 97	- 711 16	101 72 5	65 91	20
42	300	1.60	1.60	111 05	- 01 07	- 015 04	.131 /2.5	66.51	40
52	595	160			-1.31 .84	-1.3 j .20	.251 59.4		
54	333		1.26			-1.3 1 .39			
44	672		-1.03			8 h .31			
17	244		2.54	.15  .82		-1.2 g .19			
41	343	160	1.17	.09  .75	-2.01 .78	-1.6 f .25	.26  71.3	63.31	41
50	661	160	89	.11  .63	-2.4  .65	<mark>-2.2</mark>  e .40	.19  74.4	66.21	50
16	633	160	59	.10  .60	-3.2  .58	<mark>-3.2</mark>  d .33	.22  77.5	65.91	16
55	298	160	1.63	.11  .63 .10  .60 .11  .57	-2.9  .54	-3.1 c .07	.21  79.4	66.31	55
51	659	160	86	.11  .53	-3.3  .54	-3.1 b .22	.19  78.1	66.01	51
35	307	160	1.52	.11  .53 .11  .51	-3.5  .48	<mark>-3.7</mark>  a .22	.22  80.6	67.1	35
						+		+	
MEAN	521.0	160.0	.00	.10 1.03	.2 1.03	.21	50.4	49.41	

Figure 3. Item fit order output in winstep

After the item unidimensionality stage, it continues with the item fit order. To check items that are Fit and Misfit, the INFIT MNSQ value of each item is used. The average value and standard deviation are added up, then compared, a logit value greater than this value indicates item that is misfit. Other criteria according to Sumintono & Widhiarso (2015) which are used to check the suitability of inappropriate question items (Outliers or Misfits) are: 1) Acceptable Outfit Mean Square (MNSQ) value: 0.5 < MNSQ < 1.5; 2) Outfit Z-Standard (ZSTD) value received: -2.0 < ZSTD < +2.0; and 3) Point Measure Correlation (Pt Mean Corr) value received: 0.4 < Pt Measure Corr < 0.85. A valid item meets at least one of these three criteria. For example, in the first row are the output results for item number 10 on the student teacher beliefs instrument in solving mathematical problems, respectively the scores are 2.34 and 6.7 and 0.30. The third row is item number 48 whose scores are 1.60 and 2.9 and 0.20 respectively. In detail, the item fit order output is presented in Figure 3.

Validity testing by paying attention to the rating results (partial-credit) found that each rating (1, 2, 4, 5) had a separate peak. This means that the probability of each rating is clearly visible to the research respondents. Figure 4 shows clearly that the instrument for prospective teacher students' beliefs in solving mathematical problems can be differentiated in their ratings by research respondents.





The test results use item measures and variable maps to find out which items are most difficult for respondents to agree with and easiest to agree with responden (agree al., 2022; Boone, 2016; Saidi & Siew, 2019). Figure 5 shows that the Measure logit items have becars sorted from highest to lowest logit value. The 17th item with 2.54 logits shows that this item is the most difficult to agree on, while the 5th item with -2.22 logits is the item that is most easily agreed upon by respondents in the instrument of problem solving beliefs for prospective mathematics teacher students. Furthermore, taking into account the standard deviation value of 1.21, this means that the range of item difficulty levels is quite diverse so there is no need to correct it.

 
 PABLE 13.1 Keyakinan
 Dec 19 14:42 2023

 INPUT: 160 Person 60 Item REPORTED: 160 Person 60 Item 5 CATS WINSTEPS 3.73
 ----Person: REAL SEP.: 1.44 REL.: .67 ... Item: REAL SEP.: 10.52 REL.: .99

Item STATISTICS: MEASURE ORDER

NTRY	TOTAL	TOTAL		MODEL  IN	FIT   OUT	FIT	PT-MEAS	URE	EXACT	MATCH	
				S.E. MNSQ							Item
										+	
17	244	160	2.54		-1.3  .84		.19	.16	57.5	54.8	17
33	253	160	2.35	.141.95	31 .89	71	.23	.16	54.4	55.81	33
19					2 611 59	2.1	22	17	45.6	59.31	19
48	278	160	1 01	1211 62	2 011 60	2 61	20	10	50.0	62 11	49
38	287	160	1 77	1211 14	811 10	6.5	28	201	60.0	64 61	28
55	200	160	1 60	111 57	2 01 54	2.01	.20	- 201	20.0	66.01	60 66
42	290	160	1.03	.11 .57	-2.9 .04	-3.1	-07	-41	79.9	66.61	20
	300	160	1.60	.11 .00	01 .00		.04	- 44	/3.1	00.01	74
35	307	160	1.52	.11 .51	-3.5  .48	-3.7	.22	-22	80.6	67.1	35
54	333	160	1.26	.09  .85	-1.0  .81	-1.3	.39	.25	67.5	64.4	54
39	338	160	1.21	.09 1.07	.5 1.05	. 4	.20	.25	61.3	64.2	39
27	342	160	1.18	.09 1.04	.3 1.04	.3	.12	.26	63.8	63.3	27
41	343	160	1.17	.09  .75	-2.0  .78	-1.6	.25	.26	71.3	63.3	41
46	351	160	1.11	.09  .99	1  .99	.01	.31	.26	58.8	59.8	46
45	368	160	.98	.08  .99	1  .96	3	. 32	.27	56.9	55.6	45
15	374	160	.94	.08 1.04	.4 1.04	.4	.16	.28	53.1	52.1	15
21	384	160	.88	.08  .92	8 .90	9	.18	.28	50.6	46.8	21
43	398	160	.79	.13 1.73 .13 1.62 .12 1.14 .11 .57 .09 .85 .09 1.07 .09 1.04 .09 .75 .09 1.04 .09 .99 .08 .99 .08 .99 .08 .94	71.93	71	.44	. 29	39.4	37.91	43
56	402	160	.77	.08 1.12	1.311.12	1.3	. 32	.29	30.6	35.71	56
31	423	160	. 65	.0711.06	.811.08	1.0	. 22	.29	24.4	23.6	31
34	422	160	65	071 91	-1.11.91	-1.0	38	29	24.4	23 6	24
29	426	160	63	0711.21	3.611.29	3 1	. 38	20	20.0	22 5	29
1	420	160	56	.08 92 .08 94 .08 1.12 .07 1.06 .07 91 .07 1.31 .07 95 .07 1.08 .07 1.09 .07 1.01 .07 1.05 .07 1.12	- 71 05	- 61	15	201	18 1	17 71	1
47	440	160	.00	0711 09	1 1 1 1 07	0	.13	20	18.9	16 5	47
12	440	160		.0711.00	1.111.07		.01	- 491	10.0	16.01	30
	449	160	.51	.0711.09	1.3 1.00	1.1	.20	- 301	15.0	15.0	12
7	462	160	. 44	.0711.01	.211.00	.1	.37	- 29	11.9	11.5	7
6	492	160	. 29	.07 1.05	.8 1.11	1.6	14	.29	6.3	9.6	6
14			.26	.07 1.12 .07 .97 .07 .97 .07 1.05 .07 1.05 .08 1.17 .08 .85 .08 1.17 .08 .85 .08 1.11 .08 .96 .09 1.08 .10 .60	1.7 1.15	2.0	04	.29	6.3	9.3	14
22	501	160	.24	.07  .97	4 .98	3	. 22	.29	8.8	9.31	22
20	513	160 160 160	.18	.07  .97	5  .98	3	.26	.29	11.9	11.8	20
57	518	160	.15	.07 1.05	.7 1.07	.91	.14	.28	9.4	13.4	57
2	534	160	.07	.07 1.00	.0 1.07	.8	.04	.28	16.9	19.8	2
37	556	160	05	.08  .92	-1.0  .94	6	.32	.27	33.8	30.4	37
18	573	160	16	.08 1.17	1.8 1.24	2.1	.26	.26	36.9	42.3	18
52	595	160	30	.08  .85	-1.3  .84	-1.3	.20	.25	59.4	52.9	52
8	602	160	35	.0811.11	1.011.15	1.2	.15	.24	53.1	57.1	8
4	603	160	- 35	08 J . 96	- 31 .94	5	24	24	61.3	57.21	4
28	623		- 51	0911 08	611 11	8	22	221	64 4	64 81	28
16	633		- 59	101 60	-2 21 58	-2 2	22	221	77 5	65 91	16
53	634	160	60	1011.09	.6 1.09	5.5	10	201	66.0	66 01	50
26	642	160	- 69	1011 15	1 011 21	1 2	22	21	64 4	66 81	26
	643	160	00	1011.10	1.0 1.21	1.3	. 44	- 4 - 1	21.4	66.01	50
59		160	69	.10  .85 .11  .53 .11  .84 .11  .63 .11  .92	-1.01 .89	7	.28	.21	71.3	66.0	59
51	659	160	86	.11  .53	-3.3 .54	-3.1	.22	.19	78.1	00.0	51
30	660	160	87	.11  .84	9  .87	71	.16	.19	72.5	65.9	30
50	661	160	89	.11  .63	-2.4 .65	-2.2	.40	.19	74.4	66.2	50
40	666	160	95	.11  .92	4  .98	.01	.22	.19	67.5	65.7	40
44	672	160	-1.03	.12  .84 .12  .96 .12 1.14 .12  .91	9  .85	8	.31	.18	67.5	64.8	44
58	678	160	-1.11	.12  .96	2 .96	1	.29	.18	63.8	63.7	58
36	679	160	-1.13	.12 1.14	.8 1.16	. 91	.33	.17	59.4	63.5	36
25	683	160	-1.19	.12  .91	5  .93	3	.21	.17	63.8	62.6	25
32	685	160	-1.22								
60	688	160	-1 27	.131 .86	8  .88 7  .88	7	.31	.17	63.1	61.3	60
9	702	160	-1.51	.14  .88	71.88	71	.26	.16	61.9	57.6	9
49	702	160	-1.51	.1411.16	1.011.12		.29	16	58.8	57.6	49
13			-1.69	.14 1.16	411 06	4	17	15	58 1	55 41	13
10	712	160	-1 71	1412 40	6 712 24	6 7	20	15	46 0	55 21	10
3	716	160	-1.70	1511 17	1 1 1 1 10	1 9	- 30	15	50.9	54 01	2
	100	100	-1./9	.10 1.17	1.111.10	4.6	.43	.13	50.4	54.0	
23	/1/	160	-1.81	.15  .92	5  .91	6	.28	.15	60.6	04.0	23
24	723	160	-1.94	.15 1.25	1.8 1.23	1.7	.19	.15	53.1	55.4	24
11	724	160	-1.96	.14 1.06 .14 2.40 .15 1.17 .15 .92 .15 1.25 .15 1.26 .16 1.61	1.9 1.25	1.9	.17	.14	60.6	55.5	11
5	735	160	-2.22	.16 1.61	4.6 1.57	4.5	.24	.14	65.0	60.0	5
					+	+		+		+	
MEAN	521.0	160.0	.00	.10 1.03	.2 1.03	.2		1	50.4	49.4	

Figure 5. Items measure test results

#### Discussion

The instrument of student teacher beliefs in solving the mathematical problems studied can be said to be an instrument that has high reliability. Table 2 shows that the cronbach alpha interpretation is good. This shows that there is a match between the research instrument items and the research respondents. Then the consistency of the answers from respondents can be said to be sufficient with the quality of the research instrument items being excellent. This shows that the instrument of prospective teacher students' beliefs in solving mathematical problems can be said to be reliable and provides relatively stable results when used by other researchers. finstrument that has high reliability is one of the characteristics of a good instrument (Huei et al., 2020; Indihadi et al., 2022; Sharif et al., 2019; Sumintono & Widhiarso, 2015).

Table 2.	Results of	finstrument	reliability	test anal	ysis
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Cronbach	Interpreta-	Item	Interpreta-	Person	Interpreta-	Conclusion
Alpha	tion	Reliability	tion	Reliability	tion	
0.70	Good	0.99	Excellent	0.67	Fairly	Reliable

Instrument validity is used to test how far the test items are able to measure prospective teacher beliefs abilities in solving mathematical problems (Huei et al., 2020; Sumintono & Widhiarso, 2014). The validity test based on item unidimensionality shows that the total value of raw variance in observations is 57.6%. Interpretation of item unidimensionality based on the raw variance explained by measures value is indicated by a score of > 20% which is said to be fulfilled, > 40% is good and > 60% is for special criteria. Furthermore, to find out whether or not there are instrument items that do not match, you can look at the eigenvalue and observed values in the unexplained variance 1st contrast. The eigenvalue must be less than 3 to indicate that there are problematic instrument items and the observed value must be less than 15% to indicate that the instrument items are appropriate (Sumintono & Widhiarso, 2015). The results of the analysis concluded that there was no tendency for item discrepancies so that the instrument item so an item fit order analysis is carried out to determine whether the instrument item can be retained or must be discarded. A complete summary of the results of validity analysis using Winstep 3.73 software is presented in Table 3.

Raw variance explained by	Interpretation	Unexplained 1st con		Interpretation
measures		Eigenvalue	observed	
57.6%	Good	5.0	3.5%	There are problematic items

Item fit is used to explain whether the instruction normally to carry out measurements. To see whether an item fits or not, the outfit means-square, outfit z-standard, and point measure correlation values are used Huei et al., 2020; Saidi & Siew, 2019; Sharif et al., 2019; Sumintop & Widhiarso, 2015). The criteria used to check the suitability of items are: 1) Acceptable Outfit Mean Square (MNSQ) value: 0.5 < MNSQ < 1.5; 2) Outfit Z-Standard

(ZSTD) value received: -2.0 < ZSTD < +2.0; and 3) Point Measure Correlation (PT Mean Corr) value received: 0.4 < Pt Measure Corr < 0.85. An instrument item is said to be valid if it meets at least one of these three criteria. If the three criteria are met on an instrument item, it is said that the instrument item is "suitable" and it can be confirmed that the quality of the instrument item is good and can be used. However, if only two criteria or one criterion is met then the instrument item can still be maintained and does not need to be changed. Table 4 presents a summary of the results of the analysis of invalid instrument items.

Item	Statement	Outfit MNSQ	Outfit ZTSD	PT Measure Corr	Information
5	Mathematical problem solving abilities increase if you study	1.57	4.5	0.24	Invalid
10	Everyone lacks the ability to solve problems	2.34	6.7	0.30	Invalid
19	A good math teacher is one who shows students the right way to swer math questions	1.59	3.1	0.33	Invalid
35	Mathematics is a collection of processes and rules, which describe exactly how to solve a problem	0.48	-3.7	0.22	Invalid
48	A calm environment is needed for mathematics learning so that students can focus on listening to explanations of the material	1.60	2.9	0.20	Invalid

Table 4. Invalid items

In accordance with the results of the analysis that has been explained, five instrument items were obtained that did not meet the validity criteria, so it could be said that these items were invalid (Misfit) and could not be main and an explained. Overall, the development of the instrument for measuring prospective teacher beliefs in solving mathematical problems in this study was declared reliable and valid with 55 of the 60 statement items said to be valid.

Rasch modeling can help to address item measurements more consistently and correctly (Adi et al., 2022; Andrich & Marais, 2019; Boone, 2016). Another advantage of Rasch modeling is that three reliabilities are obtained, namely person reliability, item reliability, and Cronbach's alpha (Saidi & Siew, 2019; Surjetono & Widhiarso, 2015). Furthermore, through Rasch modeling it can be used to evaluate the construct validity of the instruments developed. The Rasch model is able to show instrument items that are difficult for respondents to agree on while also matching the respondent's abilities (Adi et al., 2022; Boone, 2016; Saidi & Siew, 2019). Analysis of instrument items related to the respondent's abilities is very helpful in preparing instruments to cover the aspects to be measured diukur (Kaspersen et al., 2017; Sharif et al., 2019; Sumintono & Widhiarso, 2014).

#### Conclusion

The use of Rasch modeling in instrumental alidation has produced more holistic information about the instruments being developed. Based on the test results, it was concluded that the instrument for prospective teacher beliefs in solving mathematical problems was declared reliable and valid. A total of five instrument items did not meet the validity criteria. Thus, fifty-five instrument items were obtained that can be used to measure prospective teacher students' beliefs in solving mathematical problems.

#### 12 Conflicts of Interest

The authors declare that no conflict of interest regarding the publication of this manuscript.

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